

On the Efficiency of Lobachevski-Graeffe's Method  
for Finding the Polynomial Zeros

by

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Let  $f(x) = 0$  be a nonlinear equation. The problem of determining its zeros is a very interesting and important one, existing many methods, iterative or not, see [2] - [4], to do this.

From this point of view, a special case is occupied by those nonlinear equations in which the function  $f$  is an algebraic polynomial one, with real coefficients, which can be solved by usually used methods, but also by special ones. So, in [4] is presented the Lobachevski-Graeffe's method, which can be easily translated in an serial algorithmic form.

The aim of this paper is to derive the parallel algorithm for this method and to characterize it by speedup, respectively by the efficiency point of view.

To make it possible, we suppose that a MIMD system - an arbitrary number of processors with independent control and arbitrary large memory with unrestricted access is available, (see [5]). Also, we suppose that each processor is capable to perform any of the operations  $+$ ,  $-$ ,  $\cdot$ ,  $/$ . The time required for accessing data, storing results and communicating among processors is ignored.

As it is well known, one of the characteristic of a parallel method  $E_p$  is the speedup  $S(E_p; n)$ , i.e.

$$S(E_p; n) = \frac{CP(\bar{F}_s)}{CP(E_p; n)}$$

where  $\bar{F}_s$  is the optimal serial method with regard to the complexity in a given class of such methods, (see [3]),  $CP(E_p; n)$  is the complexity of the parallel method  $E_p$  and  $n$  is the number of processors.

Using the speedup  $S(E_p; n)$ , a new characteristic for a parallel method is defined, the efficiency: