

**ON A PROPERNESS METHOD FOR FREE
VIBRATIONS PROBLEM**

Cristinel MORTICI

Abstract. This paper is concerned with the existence of nontrivial periodic solutions (free vibrations) of semilinear wave equations of the form

$$\begin{cases} u_{tt} - u_{xx} + g(t, x, u) = f(t, x) \\ u(t, 0) = u(t, \pi) = 0, & t \in \mathbf{R} \\ u(t + 2\pi, x) = u(t, x), & t \in \Omega \end{cases}$$

where $\Omega = (0, 2\pi) \times (0, \pi)$. It is used Liapunov-Schmidt method to obtain solutions of this problem as a limit of solutions of related problems in some finite dimensional spaces which can be solved. This problems will be considered with approximation schemes and corresponding mappings called approximation-proper operators.

MSC: 35L20, 35L75

Keywords: Semilinear wave equation, existence of periodic solutions