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## On $S_3$ -actions on spin 4-manifolds

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ABSTRACT. Let  $X$  be a smooth, closed, connected spin 4-manifold with  $b_1(X) = 0$  and signature  $\sigma(X)$ . In this paper we use Seiberg-Witten theory to prove that if  $X$  admits an even type symmetric group  $S_3$  action preserving the spin structure, then  $b_2^+(X) \geq |\sigma(X)|/8 + 2$  under some non-degeneracy conditions.

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