

On certain q -analogues of the Bernstein operators

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ABSTRACT.

In this note we study the limit of iterates of Lupaş q -analogue of the Bernstein operators. Also, we introduce a new class of q -Bernstein-type operators which fix certain polynomials. Both qualitative and quantitative results are established.

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