Hyperbolic-type inequalities on generalized metric spaces

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Abstract.

In this paper we consider some hyperbolic-type inequalities on generalized metric spaces. A comparison theorem and data dependence results for the solution of a Darboux problem by the Picard operators technique are given.

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