

Abstract Volterra operators

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ABSTRACT.

The aim of this paper is to study a differential equation with abstract Volterra operator. Existence and uniqueness, inequalities of Čaplygin type and data dependence (monotony, continuity) results for the solution of the Cauchy problem are obtained using weakly Picard operators theory.

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