

Some properties of generalized semirings

MARIA S. POP and ADINA POP

ABSTRACT.

The purpose of this article is to define, illustrate and study a generalization of the semirings by replacement the binary additive and multiplicative operations by others, n -ary respectively m -ary. The connections between the properties of congruences and ideals of (n, m) -semirings and the corresponding properties of its $(n, 2)$ -reduces are investigated.

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DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE
NORTH UNIVERSITY OF BAI A MARE
VICTORIEI 76, 430122 BAI A MARE, ROMANIA
E-mail address: maria.sanziana@yahoo.com
E-mail address: adina.p.2006@yahoo.com

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