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Ulam stability of a nonlinear hyperbolic partial differential equation

IOAN A. RUS and NICOLAIE LUNGU

ABSTRACT.

In this paper we present four types of Ulam stability for a nonlinear hyperbolic partial differential equations: Hyers-Ulam stability, generalized Hyers-Ulam stability, Hyers-Ulam-Rassias stability and generalized Hyers-Ulam-Rassias stability. Some examples are given.

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BABEŞ-BOLYAI UNIVERSITY
DEPARTMENT OF APPLIED MATHEMATICS
KOGĂLNICEANU 1
400084 CLUJ-NAPOCA, ROMANIA
E-mail address: iarus@math.ubbcluj.ro

TECHNICAL UNIVERSITY
DEPARTMENT OF MATHEMATICS
C. DAICOVICIU 15
CLUJ-NAPOCA, ROMANIA
E-mail address: nlungu@math.utcluj.ro

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