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Fixed point theorems for triangular operators

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ABSTRACT.

In this paper we study the existence of the fixed points for triangular operators $A : X \times Y \to X \times Y$, $A = (B, C)$, where $B : X \to X$ and $C : X \times Y \to Y$. Also, the well-posedness of the fixed point problem and the limit shadowing property are studied for this type of operators.

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