

Nonlinear multigrid methods for solving Richards' equation in two space dimensions

GH. JUNCU, A. NICOLA, C. POPA and T. UDRESCU

ABSTRACT.

We propose in this paper a nonlinear multigrid algorithm of Full Approximation Storage (MG-FAS) for efficient numerical solution of two dimensional Richards' equation modelling water infiltration into an isotropic, homogeneous, unsaturated porous medium. Comparisons with the nonlinear Alternating Line Gauss-Seidel iterations (ALGS) illustrate the much better behaviour of our solver.

REFERENCES

- [1] Bear, J. and Bachmat, Y., *Introduction to Modelling of Transport Phenomena in Porous Media*, Kluwer, Dordrecht, 1991
- [2] Broadbridge, P. and White, I., *Constant rate rainfall infiltration*, Water Resources Research **24** (1988) 145–154
- [3] Eymard, R., Gutnic, M. and Hilhorst, D., *The finite volume method for Richards' equation*, Comput. Geosciences **3** (1999) 259–294
- [4] Juncu, Gh. and Popa, C., *Introduction in the multigrid methods* (in Romanian), Ed. Tehnica, Bucharest, 1991
- [5] Lee, H. S., Matthews, C. J., Braddock, R. D., Sander, G. C. and Gandola, F., *A matlab method of lines template for transport equations*, Environ. Mod. Soft. **19** (2004) 603–614
- [6] Lehmann, F. and Ackerer, Ph., *Comparison of iterative methods for improved solutions of the fluid flow equation in partially saturated porous media*, Transp. Porous Media **31** (1998), 275–292
- [7] Loudyi, D., Falconer, R. A. and Lin, B., *Mathematical development and verification of a non-orthogonal finite volume model for groundwater flow applications*, Adv. Water Resources **30** (2007) 29–42
- [8] Marinoschi, G., *Mathematical models of nonlinear saturated-unsaturated infiltration in porous media*, Math. Rep. (Bucur.) **8** (3) (2006), 287–307
- [9] Pop, I. S., *Error estimates for a time discretization method for the Richards' equation*, Comput. Geosciences **6** (2002) 141–160
- [10] Pop, N., *An algorithm for solving nonsmooth variational inequalities arising in frictional quasistatic contact problems*, Carpathian J. Math. **24** (2) (2008), 110–119
- [11] Tocci, M. D., Kelley, C. T., Miller, C. T. and Kees, C. E., *Inexact Newton methods and the method of lines for solving Richards' equation in two space dimension*, Comput. Geosciences **2** (1998) 291–309
- [12] Wagner, C., *Numerical methods for diffusion-reaction-transport processes in unsaturated porous media*, preprint, 2007
- [13] Wagner, C., Kinzelbach, W. and Wittum, G., *Schur-complement multigrid. A robust method for groundwater flow and transport problems*, Numer. Math. **75** (1997), 523–545

POLITEHNICA UNIVERSITY
DEPARTMENT OF CHEMISTRY
78126, BUCHAREST, ROMANIA
E-mail address: juncugh@netscape.net

UNIVERSITY "OVIDIUS" UNIVERSITY
DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE
900527, CONSTANTA, ROMANIA
E-mail address: anicola@univ-ovidius.ro
E-mail address: cpopa@univ-ovidius.ro
E-mail address: tudrescu@univ-ovidius.ro

Received: 08.12.2008; In revised form: 16.03.2009; Accepted: 30.03.2009
2000 Mathematics Subject Classification. 35K55, 65N55.

Key words and phrases. Richards's equation, homogeneous unsaturated porous medium, FAS nonlinear multigrid, alternating Gauss-Seidel iteration.