

## Counting maximal chains of subgroups of finite nilpotent groups

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### ABSTRACT.

The main goal of our paper is to determine the total number of maximal chains of subgroups in a finite nilpotent group. This counting problem is reduced to finite  $p$ -groups. Explicit formulas are obtained in some particular cases.

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