A fixed point result for asymptotically nonexpansive mappings on an unbounded set

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ABSTRACT.

A result regarding the existence of a fixed point for asymptotically nonexpansive mapping defined on an unbounded subset of a Banach space is established.

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