

## Metrizable systems of autonomous second order differential equations

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### ABSTRACT.

Well-known notions from tangent bundle geometry, namely nonlinear connections and semisprays, are extended to bundle-type tangent manifolds. As main subject, the metrizability of both semisprays and nonlinear connections is investigated through Obata operators.

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