

Fixed points and invariant approximation in random normed spaces

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ABSTRACT.

Aim of this paper is to provide necessary conditions for the existence of fixed points of nonexpansive mappings on a nonconvex domain of a random normed space. As an application, related results on invariant approximation are also derived.

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