

## Existence of positive periodic solutions of functional difference equations with sign-changing terms

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### ABSTRACT.

This paper is concerned with the nonlinear functional difference equation

$$\Delta x(n) = -a(n)x(n) + \lambda h(n)f(n, x(n - \tau(n))),$$

where  $h$  and  $f$  may change sign. Sufficient conditions for the existence of at least one positive  $T$ -periodic solution are established.

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Received: 11.06.2008; In revised form: 17.11.2009; Accepted: 08.02.2010

2000 *Mathematics Subject Classification*. 34B10, 35B14.

Key words and phrases. *Positive periodic solution, functional difference equation, fixed-point theorem, sign-changing term.*