

## On some ergodic theorems for a universally bounded operator

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### ABSTRACT.

In this paper some ergodic theorems for universally bounded operators on locally convex spaces are studied. In this framework the validity of M. Lin's [10] results are proved.

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