

Generalized Weyl's theorems for polaroid operators

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ABSTRACT.

In this paper we establish necessary and sufficient conditions on bounded linear operators for which generalized Weyl's theorem, or generalized α -Weyl theorem, holds. We also consider generalized Weyl's theorems in the framework of polaroid operators and obtain improvements of some results recently established in [20] and [29].

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