

# Fixed point theorems for cyclic weak contractions in partially ordered sets endowed with a complete metric

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## ABSTRACT.

The purpose of this paper is to present some fixed point results for cyclic weak contractions in partially ordered sets endowed with a complete metric.

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