

Solvability of a second-order differential equation with integral boundary condition at resonance on an unbounded domain

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ABSTRACT.

This paper deals with the solvability of two class of second-order integral boundary value problems at resonance on a half-line. Both of the boundary value conditions are responsible for resonance. By using the coincidence degree theory, we establish a new general existence result.

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