

On some fixed point theorems for implicit almost contractive mappings

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ABSTRACT.

In this paper a general fixed point theorem for pairs of general almost contractive mappings satisfying an implicit relation is proved. In the last part of the paper is proved that the fixed point problem for these pairs of mappings is well posed.

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