

A fixed point theorem for a Ćirić-Berinde type mapping in orbitally complete metric spaces

SEONG-HOON CHO

ABSTRACT.

In this paper, we introduce the notion of Ćirić-Berinde type almost set-valued contraction mappings and give a fixed point theorem for these mappings in orbitally complete metric spaces.

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HANSEO UNIVERSITY
 DEPARTMENT OF MATHEMATICS
 CHUNGNAM, 356-706, SOUTH KOREA
 E-mail address: shcho@hanseo.ac.kr