

Superadditivity and subadditivity of some functionals with applications to inequalities

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ABSTRACT.

The superadditivity and subadditivity properties of certain composite functionals are investigated. Applications in refining Jensen's, Hölder's, Minkowski's and Schwarz's inequalities are given.

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