

Semi-linear fractional systems with Caputo type multi-step differences

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ABSTRACT.

A new class of fractional linear and semi-linear discrete-time systems described by the collection of state equations is introduced. The solution to the system is derived by the recursive formula. Presented results concern the fractional h -difference operator.

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