

Baer-Galois connections and applications

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ABSTRACT.

We define Baer-Galois connections between bounded modular lattices. We relate them to lifting lattices and we show that they unify the theories of (relatively) Baer and dual Baer modules.

Acknowledgements. This research is partially supported by the grants PN-II-RU-TE-2009-1-303 and PN-II-ID-PCE-2012-4-0100.

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Received: 24.03.2013; In revised form: 24.06.2013; Accepted: 25.06.2013
2010 *Mathematics Subject Classification.* 06A15, 16D10.

Key words and phrases. *Galois connection, bounded modular lattice, (dual) Baer module.*