Hyers-Ulam stability of some partial differential equations

NICOLAIE LUNGU and DORIAN POPA

ABSTRACT.

In this paper we obtain a Hyers-Ulam stability result for a first order partial differential equation in Banach spaces. As a consequence follows stability results for an n order partial differential equation.

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DEPARTMENT OF MATHEMATICS,
TECHNICAL UNIVERSITY OF CLUJ-NAPOCA,
MEMORANDUMULUI 28, 400114 CLUJ-NAPOCA, ROMANIA
E-mail address: nlungu@math.utcluj.ro; Popa.Dorian@math.utcluj.ro