

The theory of some asymptotic fixed point theorems

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ABSTRACT.

In this paper we present the theory about some fixed point theorems for convex contraction mappings. We give some results on data dependence of fixed points, on sequences of operators and fixed points, on well-posedness of fixed point problem, on limit shadowing property and on Ulam-Hyers stability for equations of fixed points.

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