

# A Volterra functional-integral equation, via weakly Picard operators' technique

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## ABSTRACT.

In this paper we consider a Volterra functional-integral equation with linear modifications of the arguments. We use weakly Picard operators' technique and we obtain existence and data dependence results for the solutions.

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