

Finite torsion-free rank endomorphism rings

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ABSTRACT.

We prove that a finite torsion-free rank abelian group with finite torsion-free rank endomorphism ring is a direct sum of a bounded group and a self-small group.

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