

# Oscillation of the even - order delay linear differential equation

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## ABSTRACT.

In the paper we offer criteria for oscillation of the even order delay differential equation

$$y^{(n)}(t) + p(t)y(ct) = 0$$

We provide detail analysis of the properties of this equation, we offer necessary and sufficient conditions for oscillation of studied equation and we fulfill the gap in the oscillation theory.

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