

## Factor multialgebras, universal algebras and fuzzy sets

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### ABSTRACT.

Our general investigation of universal algebras obtained from multialgebras via strongly regular equivalence relations provides useful general results concerning fuzzy set topics related to multialgebra theory. We also give many hints on how to connect our approach with the results from the literature.

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