

## Fixed point results of cyclic contractions in product spaces

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### ABSTRACT.

In this paper, the well known concept of cyclic contraction is generalized in product spaces by introducing a new class of operators called cyclic-Prešić operators. A fixed point result for such operators is proved. Some examples are given to validate the results proved herein.

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