

Fixed point results for multivalued operators with respect to a c - distance

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ABSTRACT.

In this paper we present a fixed point theorem for contractive type multivalued operators in cone metric spaces by using the concept of c -distance.

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