

# Systems of variational relations with lower semicontinuous set-valued mappings

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## ABSTRACT.

In this paper, we use fixed point techniques to establish existence criteria of the solution for a system of two variational relations with lower semicontinuous set-valued mappings.

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Received: 14.09.2014; In revised form: 09.01.2015; Accepted: 31.01.2015

2010 Mathematics Subject Classification. 49J40, 49J53.

Key words and phrases. System of variational relations, set-valued mapping, fixed point.

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