

Fixed point theorems for cyclic non-self single-valued almost contractions

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ABSTRACT.

Let X be a Banach space, A and B two non-empty closed subsets of X and let $T : A \cup B \rightarrow X$ be an operator. We define the notion of cyclic non-self almost contraction and we give a corresponding fixed point theorem.

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