

# Common fixed points for an uncountable family of weakly contractive operators

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## ABSTRACT.

In this paper, we consider some behavior concerning common fixed points of an uncountable family of operators. We apply here the concept of circular metric spaces, and the operators are assumed to satisfy different rates of weak contractivity. We show under certain assumptions that weakly contractive family have some strong relationships to its common selector in terms of their fixed points.

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