

Common fixed points of two finite families of nonexpansive mappings by iterations

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ABSTRACT.

We study a Mann type iterative scheme for two finite families of nonexpansive mappings and establish Δ -convergence and strong convergence theorems. The obtained results are applicable in uniformly convex Banach spaces (linear domain) and CAT (0) spaces (nonlinear domain) simultaneously.

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