

Some fixed points results on Branciari metric spaces via implicit functions

ERDAL KARAPINAR ^{1,2}

ABSTRACT.

In this paper, we introduce the notion of α -implicit contractive mapping of integral type in the context of Branciari metric spaces. The results of this paper, generalize and improve several results on the topic in literature. We give an example to illustrate our results.

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¹ DEPARTMENT OF MATHEMATICS, ATILIM UNIVERSITY
06836 INCEK, ANKARA-TURKEY

² NONLINEAR ANALYSIS AND APPLIED MATHEMATICS RESEARCH GROUP (NAAM)
KING ABDULAZIZ UNIVERSITY, JEDDAH, SAUDI ARABIA

E-mail address: erdal.karapinar@yahoo.com, erdal.karapinar@atilim.edu.tr