

A general convergence theorem for multiple-set split feasibility problem in Hilbert spaces

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ABSTRACT.

We establish strong convergence result of split feasibility problem for a family of quasi-nonexpansive multi-valued mappings and a total asymptotically strict pseudo-contractive mapping in infinite dimensional Hilbert spaces.

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