Fixed point theorems for correspondences with properties weaker than lower semicontinuity

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ABSTRACT.

In this paper, we study existence of fixed points for correspondences having weak continuity properties. The obtained results extend or improve the corresponding results present in literature. We use continuous selection technique and also well-known KKM principle in order to establish our fixed point theorems.

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