

On α -nonexpansive mappings in Banach spaces

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ABSTRACT.

In 2011 Aoyama and Kohsaka introduced the α -nonexpansive mappings. Here we present a further study about them and their relationships with other classes of generalized nonexpansive mappings.

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