

On the uniform convergence of a q -series

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ABSTRACT.

The paper deals with a class of linear positive operators expressed by q -series. By using modulus of smoothness an upper bound of approximation error is determined. We identify functions for which these operators provide uniform approximation over noncompact intervals. A particular case is delivered.

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