

The iterates of positive linear operators with the set of constant functions as the fixed point set

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ABSTRACT.

Let $\Omega \subset \mathbb{R}^p$, $p \in \mathbb{N}^*$ be a nonempty subset and $B(\Omega)$ be the Banach lattice of all bounded real functions on Ω , equipped with *sup norm*. Let $X \subset B(\Omega)$ be a linear sublattice of $B(\Omega)$ and $A: X \rightarrow X$ be a positive linear operator with constant functions as the fixed point set. In this paper, using the weakly Picard operators techniques, we study the iterates of the operator A . Some relevant examples are also given.

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