

## Some additive results for the $Wg$ -Drazin inverse of Banach space operators

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### ABSTRACT.

We investigate additive properties of  $Wg$ -Drazin inverse of two  $Wg$ -Drazin invertible linear operators in Banach spaces under the commutative case. These results generalize recent works on the Drazin inverse of complex matrices.

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