

Error estimates for approximating best proximity points for cyclic contractive maps

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ABSTRACT.

We find a priori and a posteriori error estimates of the best proximity point for the Picard iteration associated to a cyclic contraction map, which is defined on a uniformly convex Banach space with modulus of convexity of power type.

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