

Dedicated to Professor Emeritus Ioan A. Rus on the occasion of his 80th anniversary

Examples of cyclical operators

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ABSTRACT.

In this paper, we give examples of cyclic operators defined on various types of sets, in order to illustrate some results in the extremely rich literature following the seminal paper [Kirk, W. A., Srinivasan, P. S. and Veeramani, P., *Fixed points for mappings satisfying cyclical contractive conditions*, Fixed Point Theory, **4** (2003), No. 1, 79 – 89]. All examples which are presented enrich the list of cyclic operators and give a subject to future studies of this type of operators.

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