

Dedicated to Professor Emeritus Ioan A. Rus on the occasion of his 80<sup>th</sup> anniversary

## Fixed point theorems for nonself $G$ -almost contractive mappings in Banach spaces endowed with graphs

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### ABSTRACT.

In this paper, we prove some fixed point theorems for non-self  $G$ -almost contractive mappings in Banach spaces with a directed graph and give some examples to illustrate our main results. The main results in this paper extend and generalize many known results in the literature therein.

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