

Stability in non-autonomous periodic systems with grazing stationary impacts

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ABSTRACT.

This paper examines impulsive non-autonomous periodic systems whose surfaces of discontinuity and impact functions are not depending on the time variable. The W -map which alters the system with variable moments of impulses to that with fixed moments and facilitates the investigations, is presented. A particular linearization system with two compartments is utilized to analyze stability of a grazing periodic solution. A significant way to keep down a singularity in linearization is demonstrated. A concise review on sufficient conditions for the linearization and stability is presented. An example is given to actualize the theoretical results.

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