

Existence and nonexistence of positive solutions to a discrete boundary value problem

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ABSTRACT.

We study the existence and nonexistence of positive solutions for a system of nonlinear second-order difference equations subject to coupled multi-point boundary conditions which contain some positive constants.

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