

Linear representation of Abel-Grassmann groups

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ABSTRACT.

We describe a linear representation for Abel-Grassmann groups. As a consequence, we obtain or improve many previous results. For example, we calculate the number of Abel-Grassmann groups of order < 512 up to isomorphism.

Acknowledgements. Partly supported by the GAČR grant 13-01832S

REFERENCES

- [1] Ahmad, I., Rashad, M. and Shah, M., *Constructions of some algebraic structures from each other*, Int. Math. Forum 7, (2012), No. 53-56, 2759–2766
- [2] Cho, J. R., Ježek, J. and Kepka, T., *Paramedial groupoids*, Czech. Math. J., **49** (1999), No. 2, 277–290
- [3] Dudek, W. and Gigoń, R., *Congruences on completely inverse AG^{**} -groupoids*, Quasigroups Relat. Syst., **20** (2012), No. 2, 203–209
- [4] Dudek, W. and Gigoń, R., *Completely inverse AG^{**} -groupoids*, Semigroup Forum **87**, (2013), No. 1, 201–229
- [5] The GAP Group, *GAP – Groups, Algorithms, and Programming, Version 4.5.7*, 2012, (<http://www.gap-system.org>)
- [6] Gumm, H. P. and Ursini, A., *Ideals in universal algebras*, Algebra Universalis, **19** (1984), 45–54
- [7] Ježek, J. and Kepka, T., *Medial groupoids*, Rozprawy ČSAV, Rada mat. a přír. věd 93/2, 1983, 93 pp.
- [8] Kamran, M. S., *Conditions for LA-semigroups to resemble associative structures*, Ph. D. Thesis, Quaid-i-Azam Universiti, Islamabad, 1993
- [9] Khan, M. and Anis, S., *An analogy of Clifford decomposition theorem for Abel-Grassmann groupoids*. Algebra Colloq., **21** (2014), No. 2, 347–353
- [10] Němec, P. and Kepka, T., *T-quasigroups I*, Acta Univ. Carolin. Math. Phys., **12** (1971), No. 1, 39–49
- [11] Monzo, R. A. R. *On the structure of completely inverse AG^{**} -groupoids*, <https://arxiv.org/abs/1502.06516>
- [12] Mushtaq, Q. and Kamran, M. S., *On left almost groups*, Proc. Pak. Acad. of Sciences, **33** (1996), 1–2
- [13] Mushtaq, Q. and Khan, K., *Semilattice decomposition of locally associative AG^{**} -groupoids*, Algebra Colloq., **16** (2009), 17–22
- [14] Protić, P., *Congruencies on an inverse AG^{**} -groupoid via the natural partial order*, Quasigroups and Related Systems, **17** (2009), No. 2, 283–290
- [15] Protić, P., *Some remarks on Abel-Grassmann's groups*, Quasigroups and Related Systems, **20** (2012), 267–274
- [16] Shah, M. and Ali, A. *Some structural properties of AG -groups*, Int. Math. Forum, **6** (2011), No. 33–36, 1661–1667
- [17] Shah, M., Gretton, C. and Sorge, V., *Enumerating AG -groups with a study of Smaradache AG -groups*, Int. Math. Forum, **6** (2011), No. 61–64, 3079–3086
- [18] Toyoda, K., *On axioms of linear functions*, Proc. Imp. Acad. Tokyo, **17** (1941), 221–227

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Received: 02.02.2017; In revised form: 08.06.2017; Accepted: 17.06.2017

2010 Mathematics Subject Classification. 20N05, 20N02.

Key words and phrases. Abel-Grassmann group, AG^{**} -groupoid, paramedial quasigroup, affine representation.