

Robust vector optimization with a variable domination structure

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ABSTRACT.

In this paper we propose a new definition of robustness for uncertain vector-valued optimization problems equipped with a variable domination structure, derive scalarization results and present algorithms for computing robust solutions.

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